Balanced Billing Cycles and Vehicle Routing of Meter Readers

by

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Preface: My Dissertation Research

- Involved large-scale vehicle routing
- Partially supported by the American Newspaper Publishers Association (from January 1974 to June 1975)
 - Develop a computer code for specifying vehicle routes for bulk newspaper deliveries
 - ➤ Determine if these computerized approaches look promising
- We worked with the Worcester Telegram (WT)
 - Evening circulation of 92,000, approximately 600 drop points
 - > We located the depot and drop points on a large map with pins
 - > We used Euclidean distances and generated routes quickly

Transition from Ph.D. Student to Consultant

- Next, we compared our routes to existing WT routes
- WT re-examined their routes and altered several
- The experiment was reasonably successful and fun
- Larry Bodin and I started at the University of Maryland in 1976
- Arjang Assad and Mike Ball arrived in 1978
- In 1978 and 1979, the four of us worked for Scientific Time Sharing Corp. (STSC) on two projects involving vehicle routing
- We worked with Donald Soults at STSC
- The projects were exciting, but STSC got most of the money
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Founding and Running a Consulting Company

- Assad, Ball, Bodin and Golden founded RouteSmart in 1980
- In the 1980s, we consulted with large companies on vehicle routing
- Starting in 1989, we designed and sold vehicle routing software
- In 1998, we sold the business to a large NY civil engineering company
- We remained connected to RouteSmart until early 2004
- RouteSmart Technologies, Inc. is currently run by Larry Levy – my newspaper boy in 1978 & 1979
- RouteSmart has major installations in the newspaper, utility, waste/sanitation, and postal/local delivery industries

The Billing Cycle Vehicle Routing Problem

- This problem was described to us by RouteSmart Technologies— it applies to all utility companies
- Over time, a utility company's meter-reading routes become inefficient, imbalanced, and fractured
- Utilities wish to remedy this situation by shifting customers to different billing days and routes subject to certain constraints
- We began with a real-world data set of 17,775 customers

Imbalanced Routes

- Each customer is assigned to one of 20 billing days
- Three meter readers are working each day
- The number of customers visited each day varies between 400 and 1300
- Daily route length varies widely also
- A utility company in this situation has several goals and constraints

Goals and Constraints

- Create more efficient routes for each day of the billing cycle
- Balance the workload across the billing cycle, in terms of customers serviced and total route length
- Regulatory and customer service considerations prevent the utility company from shifting a customer's billing day by more than a few days from one month to the next
- These were put in place to eliminate variation in customers' bills due to utility company policies

A Simplified Problem as a First Step

- Let's start with a smaller and easier problem
- Simplifying assumptions
 - > 1000 customers and a 10 day billing cycle
 - We suppress the street network and treat this as a node routing problem in Euclidean space
 - ➤ One meter reader working per day
 - Each billing day corresponds to one route

Approaches to the Problem

- We see two approaches to this problem
 - ➤ Iterative and targeted
- Iterative approach
 - ➤ We take the existing configuration and improve it as much as we can from one period to the next
- Targeted approach
 - ➤ We create an idealized set of efficient, balanced routes for each day
 - Next, we attempt to transition to these routes over a small number of intermediate periods

Outline of a Heuristic Algorithm

- We selected a three-step targeted approach
- 1. Ignore all of the customers' current billing days and construct a balanced and efficient set of *target routes*
 - One target route per billing day
 - Each target route contains a set of customers with different original billing days
- 2. Assign a single billing day to each target route, attempting to minimize the number of customers that must endure a large billing day change
- 3. Construct routes for transitional periods that allow us to move from the initial configuration to the target routes while obeying the billing day shift constraints

Step 1: Construct Balanced Routes

- For the set of 1000 customers, create a set of 10 balanced routes
- First, generate an initial solution with the desired number of routes (10 in our case)
- We use improvement operators that affect at most two routes at a time
- For inter-route moves, consider the differences in route lengths and number of customers in each route
- We reward moves that decrease both of these differences and penalize moves that increase both

Step 1: Construct Balanced Routes

- We construct balanced routes as follows
- 1. Generate an initial solution using Clarke-Wright algorithm
- 2. Improve using a record-to-record travel algorithm and traditional savings until we reach a solution with the desired number of routes
 - ➤ Uses relocate, swap, and two-opt moves within and between routes
- 3. Run the same record-to-record travel algorithm, but now penalizing and rewarding certain inter-route moves

Step 1: Construct Balanced Routes

An example

- ≥ 10 vehicles and 1000 customers
- Some balance enforced by $N(R) \le 110$

What happens as we vary the balance parameter α

α	Total Route Length	(Min, Max, SDev) Route Length	(Min, Max, SDev) # in Route
0	2584	(76, 374, 82)	(37, 110, 22.6)
0.5	2561	(161, 366, 69)	(81, 110, 10.8)
0.99	2632	(205, 307, 33.5)	(90, 110, 7.4)

Step 2: Assign Billing Days to the Routes

- Following Step 1, each route corresponds to a single, final billing day
- Each of these routes contains a mix of customers with different original billing days
- We define $||a, b||_D$ to be the billing distance between days a and b, i.e., the number of days separating a and b, allowing for wraparounds in a D-day cycle
- For example, $||9, 1||_{10} = 2$

Step 2: Assign Billing Days to the Routes

Given a max billing day shift of M days, the cost of assigning billing day j to customer i with original billing day d(i) is defined as

$$c_{ij} = \begin{cases} 0 & \text{if } ||d(i), j||_D \le M \\ ||d(i), j||_D & \text{otherwise} \end{cases}$$

This cost function rewards billing day assignments that enable us to immediately assign a customer to the final billing day

Step 2: Assign Billing Days to the Routes

- The cost of assigning billing day j to an entire target route R is the sum $\Sigma_{i \in R} c_{ij}$ of these billing shift costs for each customer in the route
- We then determine final billing days for each target route by solving an Assignment Problem using this cost function
- The table below shows the Assignment Problem solution as we change the maximum allowed shift size *M*

	Target Route 1	Target Route 2
	(1, 1)	(1, 13)
Original Billing	(4, 36)	(3, 19)
Day Mixture	(7, 41)	(4, 37)
	(9, 24)	
M = 1	5	3
M=2	5	3
M=3	6	2

- We now have an initial set of billing days and routes and a set of final target routes with each route assigned a single, final billing day
- The next task is to create routes for the transition periods, while observing the billing day shift constraint
- First, include all customers that can be moved to their final billing day in a single shift
- We refer to these routes as *skeleton routes*, each of which contains a subset of the customers included in the associated target route

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- In our 1000-node example, the skeleton routes contain 825 of the 1000 nodes
- The remaining 175 customers will be transitioned to their final billing days via a sequence of intermediate billing days
- We solve a series of Generalized Assignment
 Problems in which we consider a single shift at a time for each customer
- This is similar to a Transportation Problem
 - The *supply* nodes are the customers not yet assigned to their final billing day
 - The *demand* nodes represent the skeleton routes

- For each unassigned customer i and each skeleton route j, we define c_{ij} to be the cost of inserting i into route j
- Note that for each skeleton route j, the value $\sum_{i \in R} c_{ij} x_{ij}$ is an upper bound on the increase to the total length of route j
- We try to use this upper bound as a constraint in the formulation by repeatedly solving an IP with a tighter and tighter bound
- We also introduce constraints to bound the number of customers inserted into any skeleton route

- Let L_j be the current length of skeleton route j and let N_j be the number of customers on this route
- Let T_{min} and T_{max} denote the minimum and maximum number of customers allowed on a route
- Let f(i) denote the final billing day of customer i
- Let $x_{ij} = 1$ if customer *i* is inserted into route *j*
- We set the bound B to a large value, such as twice the maximum allowed route length

Step 3: Solving the Integer Program

$$\min \sum_{i,j} c_{ij} x_{ij}$$

$$\sum_{j} x_{ij} = 1 \ \forall i$$

$$L_{j} + \sum_{ij} c_{ij} x_{ij} \leq B \ \forall j$$

$$T_{min} \leq N_{j} + \sum_{ij} c_{ij} \leq T_{max} \ \forall j$$

$$x_{ij} = 0, \text{ if } ||d(i), j||_{D} > M$$

$$x_{ij} = 0, \text{ if } ||j, f(i)||_{D} > ||d(i), f(i)||_{D}$$

$$x_{ij} \in \{0, 1\}$$

- Upon finding the smallest value of B for which a solution exists, the x_{ij} variables indicate how to construct the routes for each intermediate period from the skeleton routes
- Upon making these insertions, more customers are now assigned to their final billing days
- Resolve the problem for the customers who are still not assigned to their final billing day
- The algorithm terminates when all customers are assigned to their final billing day

Some Observations

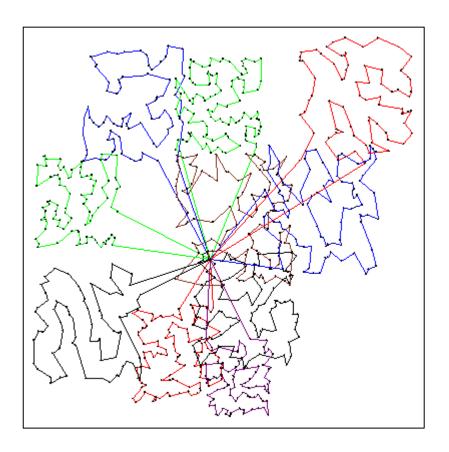
- The final constraint on page 18 requires that we always move a customer *closer* to its final billing day
- The maximum initial billing distance is [D/2]
- Therefore, the constraint guarantees that we will need at most [D/2]-1 intermediate periods

A Fully Worked-out Example (M = 2)

	Total length	# customers assigned to correct final billing day
Original routes	3168	59
1 st transitional per.	3371	825
2 nd transitional per.	2803	895
3 rd transitional per.	2746	982
Target routes	2632	1000

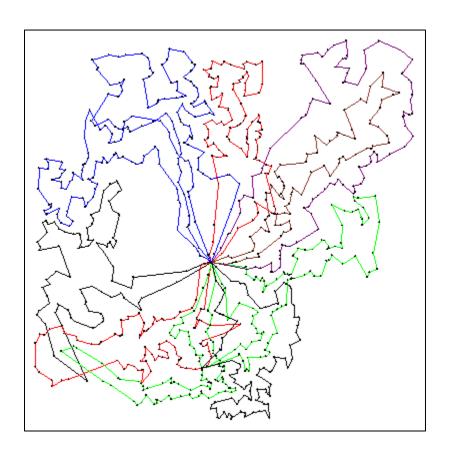
Original Routes

Total length = 3168



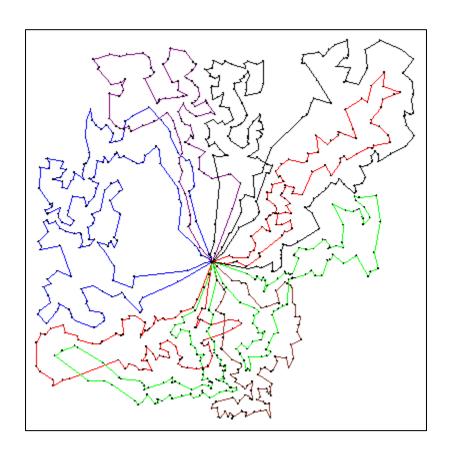
Intermediate Routes

Total length = 2803



Target Routes

Total length = 2632



Conclusions

- Our algorithm combines VRP metaheuristics with IP to create high-quality solutions
- One of the interesting complications is that we are forced to start with an initial configuration that can be very poor
- Future work: Perform more extensive computational experiments